

## **Maximum Boost control of Cascaded MultiLevel Z-Source Inverter for Fuel Cell Applications**

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**Abstract**—In this paper, a cascaded five level Z-Source inverter is proposed for fuel cell applications. The proposed topology employs Z network between the DC source and inverter circuitry to achieve boost operation. The output voltage of proposed inverter can be controlled using modulation index and shoot through state. Various modulation strategies have been reported in the literature for the proposed topology. But this paper focuses on the implementation of maximum boost control with third harmonic injection which turns all traditional zero states into shoot-through states. The performance parameters of Z-Source cascaded Multilevel inverter is computed and compare with simple boost method. Simulations of the circuit configuration of the control methods have been performed in MATLAB/Simulink and the results are verified.

**Keywords**—Cascaded Z-source Multilevel Inverter, Maximum boost control, voltage stress & voltage gain..

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### **I. INTRODUCTION**

In recent years, the multilevel voltage inverter is widely used in high power applications such as large induction motor drives, UPS systems and Flexible AC Transmission Systems (FACTS). Multilevel inverter obtains a desired output voltage from several levels of input DC voltage sources. With an increasing number of DC voltage sources, the inverter voltage output waveform level increases. As compared to traditional two level inverters, the multilevel inverters have more advantages which include lower semiconductor voltage stress, better harmonic performance, low Electro Magnetic Interference (EMI) and lower switching losses. Despite these advantages, multilevel inverters output voltage amplitude is limited to DC sources voltage summation. Occurring of short circuit can destroy multilevel inverters. To solve these problems, cascaded multilevel Z-source inverter [1-2] is proposed in this paper. The performance of the inverter is analyzed by employing a maximum boost control with third harmonic injection PWM technique. Maximum boost control converts all traditional zero states to shoot through while maintaining the active states. In this technique, the shoot through duty ratio varies during each cycle and maximum gain is obtained. Simple boost and maximum boost control methods for the proposed inverter topology are analyzed and compared. The effect of voltage gain and voltage stress for various modulation indices is studied for both the methods and the results are verified.

### **II. CASCADED MULTILEVEL Z-SOURCE INVERTER**

The circuit diagram of cascaded Z-Source five-level inverter is shown in Fig.1. It consists of a series single phase H bridge inverter units, Z impedances and DC voltage sources. DC sources can be obtained from batteries, fuel cells, solar cells [1]. Each H-bridge Z-Source inverter can generate three different output voltage +Vin, 0, -Vin. Output voltage can be higher than the input voltage when boost factor,  $B > 1$ . The number of output voltage levels,  $m$  in this topology is given by  $(n-1)/2$ , where  $n$  is the number of Z impedances or DC voltage sources. This topology has an extra switching state: shoot through state as compared to cascaded H-bridge inverters. During the shoot-through state, the output voltages of Z networks are zero [3].

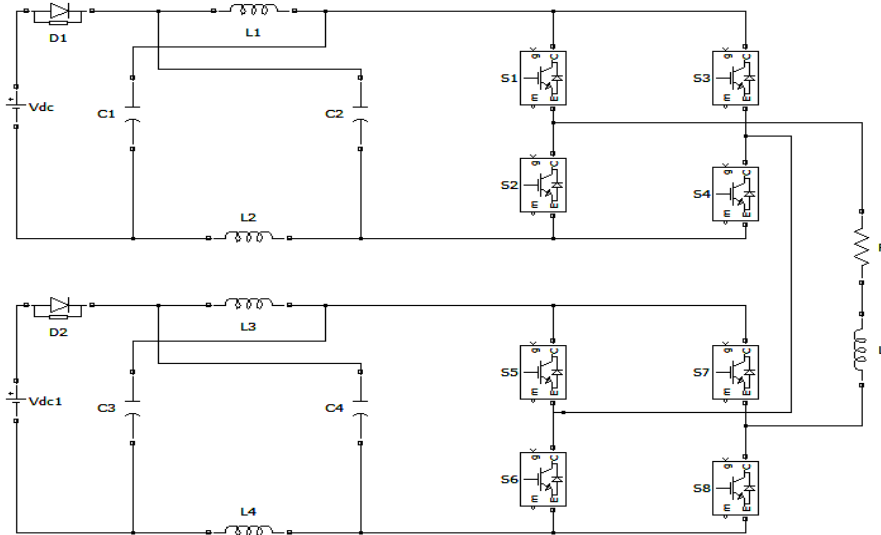


Fig.1. Five-level cascaded Z-source Multilevel Inverter

Circuit operation consists of two modes namely shoot-through and non shoot-through states [2]. In Shoot-Through (ST) switching state of Z-Source MLI, upper and lower bridges of the same leg is turned on having the output voltage of zero. During non shoot-through state opposite pairs of legs of both the bridge conducts. In ST state the two inductors are being charged by the capacitors and in Non-Shoot-Through (NST) states the inductors and input DC source transfer energy to the capacitors and load. This process is similar to the boost converter. Output voltage depends on the boost factor. The conduction table is shown in table –I

Table –I Conduction Table for Cascaded Multilevel Z-source Inverter

VOLTAGE LEVEL OUTPUT	VOLTAGE	ON SWITCHES
Level 2 (non shoot-through)	$2V_{in}$	$S_3, S_4, S_5, S_6$
Level 1 (non shoot-through)	$V_{in}$	$S_1, S_3, S_5, S_6$
Level 1 (shoot-through)	$V_{in}$	$S_1, S_2, S_3, S_4, S_5, S_6$
Level 1 (non shoot-through)	$V_{in}$	$S_3, S_4, S_5, S_7$
Level 1 (shoot-through)	$V_{in}$	$S_3, S_4, S_5, S_6, S_7, S_8$
Level 0 (zero state)	0 (V)	$S_1, S_3, S_5, S_7$
Level 0 (shoot-through)	0 (V)	$S_1, S_2, S_3, S_4, S_5, S_7$
Level 0 (shoot-through)	0 (V)	$S_1, S_3, S_5, S_6, S_7, S_8$
Level -1 (non shoot-through)	$-V_{in}$	$S_1, S_3, S_7, S_8$
Level -1 (shoot-through)	$-V_{in}$	$S_1, S_2, S_3, S_4, S_7, S_8$
Level -1 (non shoot-through)	$-V_{in}$	$S_1, S_2, S_5, S_7$
Level -1 (shoot-through)	$-V_{in}$	$S_1, S_2, S_5, S_6, S_7, S_8$
Level -2 (non shoot-through)	$-2V_{in}$	$S_1, S_2, S_7, S_8$

### III. MAXIMUM BOOST CONTROL WITH THIRD HARMONIC INJECTION

A simple third harmonic injection method is therefore presented to provide the waveform with high quality. The reference waveform consists of both fundamental component and third harmonic component. The sinusoidal reference signal can be injected by a third harmonic with a magnitude equal to 25% of the fundamental. As a result, the peak-to-peak amplitude of the resulting reference function does not exceed the DC supply voltage  $V_s$ , but the fundamental component is higher than the available supply  $V_s$ . This eliminates third and multiples of third order harmonics which leads to reduction in Total Harmonic Distortion it is observed that Third harmonic injection PWM technique gives high voltage gain and reduced THD. Inductor current ripple and capacitor voltage ripple of Z-Source cascaded inverter are also reduced. Therefore, third harmonic injection PWM technique. Maximum boost control with third harmonic injection turns all traditional zero states

into shoot-through state [4-6]. The voltage stress across the switching devices is greatly reduced by fully utilizing the zero states. Turning all zero states into shoot-through state can minimize the voltage stress and this causes a shoot-through duty ratio varying in a line cycle, which causes inductor current ripple.

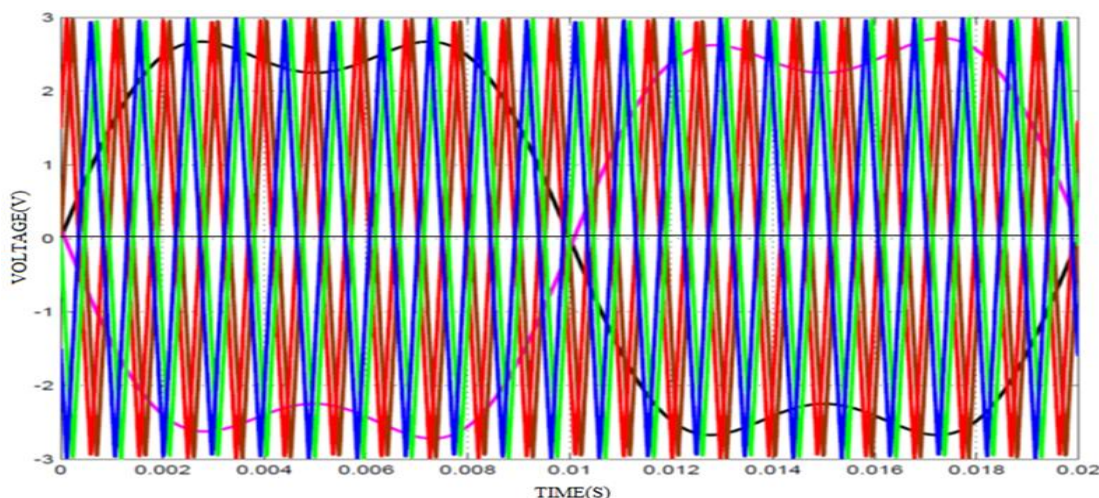
Maximum shoot-through boost factor can be written as,

$$B = \frac{1}{1-2D} \quad (1)$$

Where B is boost factor and D is duty ratio which is given by

$$D = \frac{2\pi - 3\sqrt{3}\pi}{2\pi} \quad (2)$$

The circuit is in shoot through state when the triangular carrier wave is either greater than the maximum curve of the reference signals or smaller than the minimum of the references [7,8]. The shoot-through duty cycle varies each cycle. The shoot-through state repeats periodically in every  $n/3$  degrees. Fig.2 shows the reference and carrier waveforms for maximum boost control with third harmonic injection PWM technique. The circuit is in shoot through state when the triangular carrier wave is either greater than the maximum curve of the reference signals or smaller than the minimum of the references. The shoot-through duty cycle varies each cycle.



**Fig.2** Maximum Boost control with third harmonic injection

Fig.3 shows Matlab/ Simulink of Z-Source cascaded MLI using Unipolar PWM with Boost factor = 1.25,  $m_a = 0.8$ , RL Load where  $R=50\Omega$  and  $L=24mH$ , Input voltage  $V_{dc}=75V$ , Z impedances,  $L_1 = L_2 = L_3 = L_4 = L = 40mH$  and  $C_1 = C_2 = C_3 = C_4 = 6600\mu F$ . Simulink circuit is shown with LC filter having  $L=30mH$  and  $C=150\mu F$ .

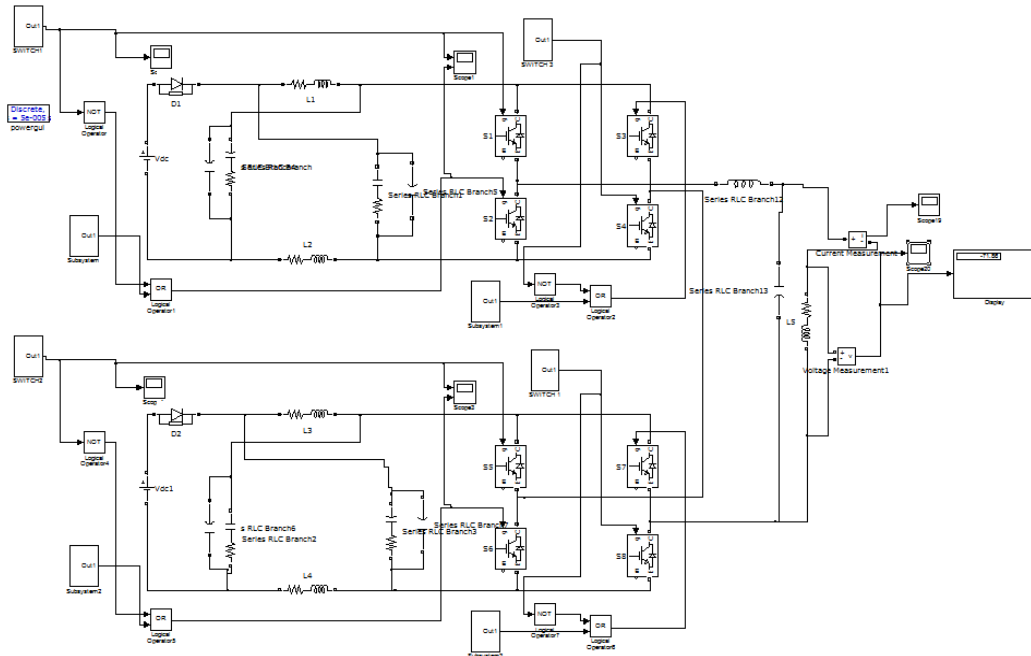


Fig 3 MATLAB/ SIMULINK circuit of Z-Source cascaded MLI using Maximum Boost control

#### IV. SIMULATION OF CASCADED Z-SOURCE INVERTER USING MAXIMUM BOOST CONTROL WITH THIRD HARMONIC INJECTION

The simulation results for the Z-source MLI with maximum boost control is shown in Figs.4,5 &6.

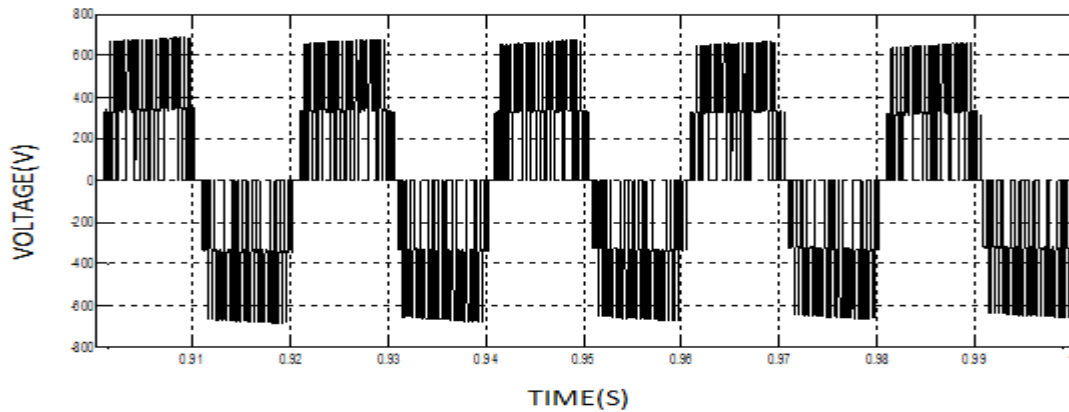


Fig.4 Load voltage waveform for maximum boost control with Third Harmonic injection PWM without filter (Boost factor: 3.09,  $m_a=0.8$ , RL Load)

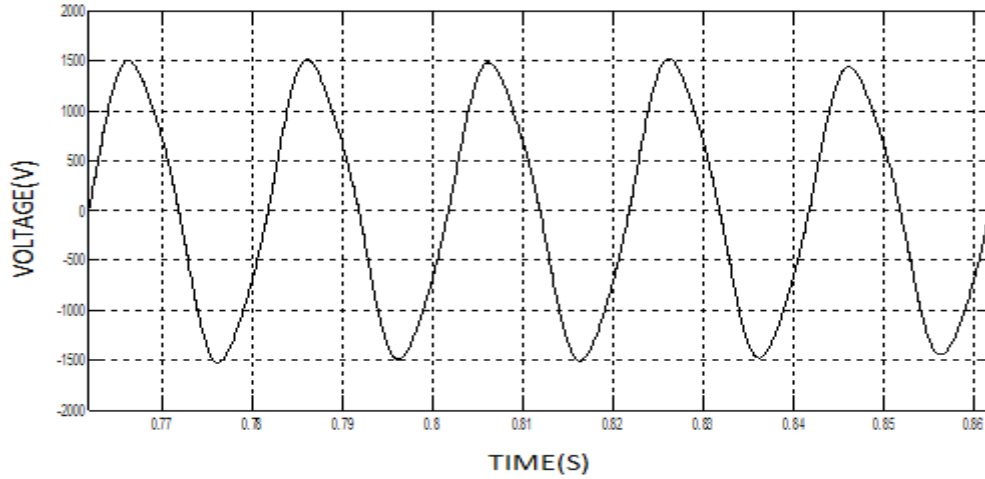


Fig 5. Filtered output voltage waveform for Z-Source MLI

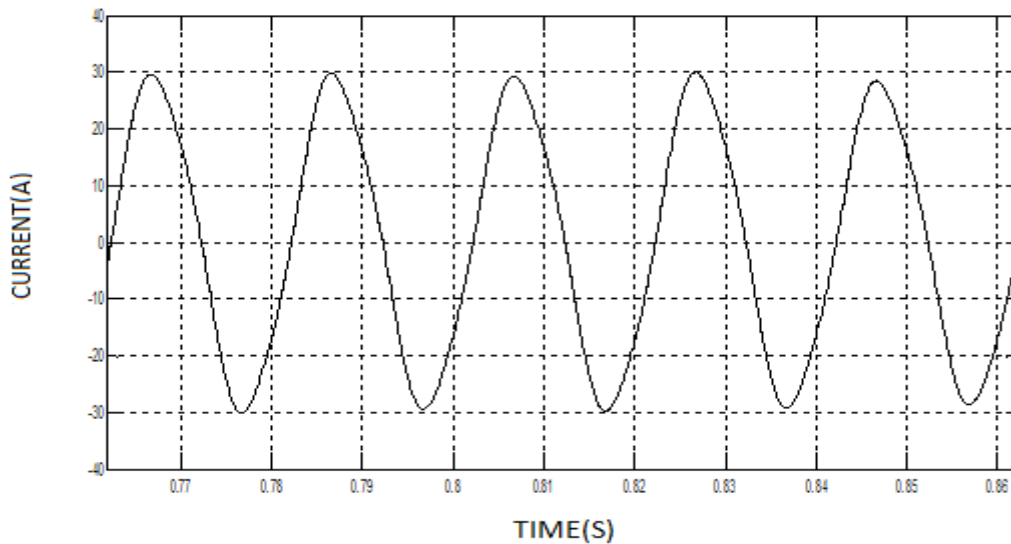


Fig .6 Filtered output current waveform for Z-Source MLI

Performance parameters of Z -Source multilevel Inverter are analyzed for various control methods which are implemented using third harmonic injection PWM technique [9-12]. Performance parameters are Total Harmonic Distortion, inductor current ripple of Z-Source inverter, capacitor voltage ripple of Z-Source inverter, voltage gain and voltage stress. Total Harmonic Distortion of five level Z-Source inverter is analyzed and compared for control methods- -simple boost control and maximum boost control. THD is calculated for various modulation index values and the comparison is shown in Fig.7.

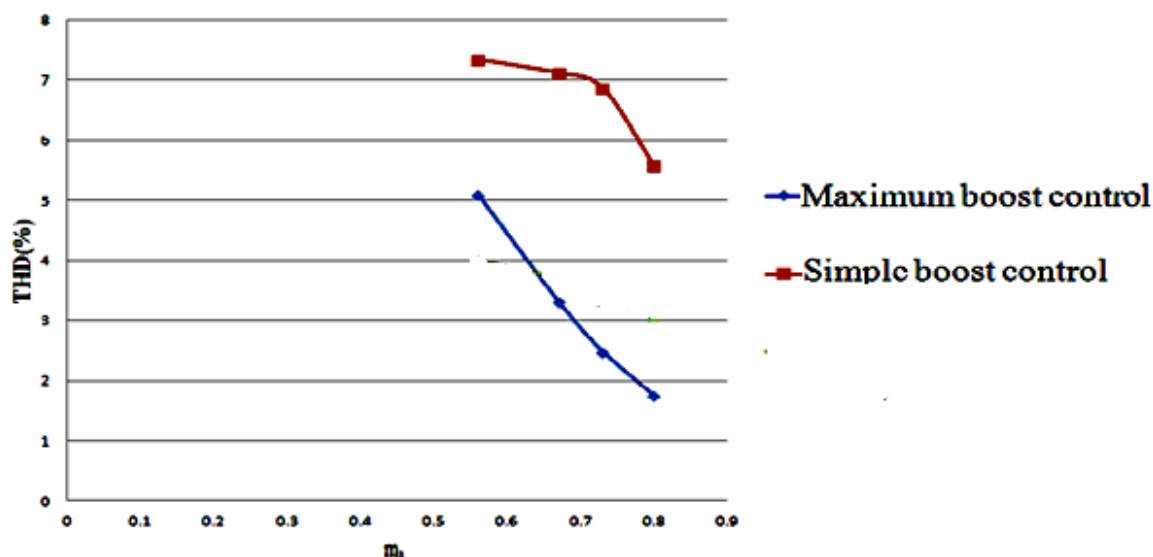


Fig .7 Effect of modulation index on Total Harmonic Distortion for three control techniques

From Fig .7, it can be concluded that the maximum boost control technique has reduced THD<sub>v</sub> compared to simple boost for m<sub>a</sub>=0.8. Inductor current ripple is calculated across the inductor of z impedance of Z-Source inverter. Inductor current ripple is shown in table for various modulation strategies that changes with variation in modulation indices.

Table I Effect of modulation index on inductor current ripple for three control techniques

S.NO	m <sub>a</sub>	SIMPLE BOOST CONTROL METHOD	MAXIMUM BOOST CONTROL METHOD
1	0.8	0.5	0.0598
2	0.73	0.6191	0.0680
3	0.67	0.7	0.0796

From the Table I, it is clear that maximum boost control has less inductor current ripple than simple boost control method. Capacitor voltage ripple is calculated across the capacitor of z impedance of Z-Source inverter. Capacitor voltage ripple is shown in table -II for various modulation strategies that changes with variation in modulation indices.

Table II Effect of modulation index on Capacitor voltage ripple for three control techniques

S.NO	m <sub>a</sub>	SIMPLE BOOST CONTROL METHOD	MAXIMUM BOOST CONTROL METHOD
1	0.8	0.0414	0.1138
2	0.73	0.0362	0.8718
3	0.67	0.0230	0.8571

From the Table II, maximum boost control has the least capacitor voltage ripple which reduces the cost of the capacitor used. Voltage gain, G is calculated for various modulation strategies. In Fig.8, voltage gain in compared with different modulation indices for all modulation techniques. Voltage gain, G is given by [13,14],

$$G = \frac{2V_{ac}}{V_{in}} \quad (3)$$

where, V<sub>ac</sub>=RMS value of output voltage  
V<sub>in</sub>=Input voltage

From the Fig 8 , maximum boost control technique has higher voltage gain compared to simple boost control method for  $m_a=0.8$ .

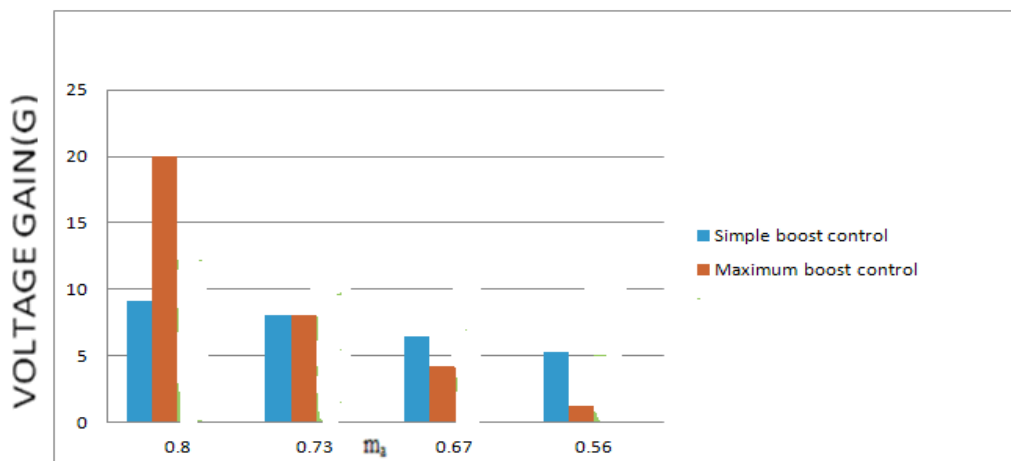


Fig 8 Effect of modulation index on voltage gain for three control techniques

In Figures 8, 9 and 10, voltage stress is compared with voltage gain for various modulation techniques. Voltage Stress is calculated from voltage gain as shown in equations (4-6). Voltage Stress is given by [15],

Simple boost control: - 
$$V_s = 2 - \frac{1}{G} \quad (4)$$

Maximum boost control: - 
$$V_s = \sqrt{3} - \frac{1}{G} \quad (5)$$

Maximum constant boost control: - 
$$V_s = \frac{\Pi}{3\sqrt{3}G - \Pi} \quad (6)$$

Where, G=Voltage gain

Fig.9 to Fig.10 shows variation of voltage stress with voltage gain(G) for all three techniques.

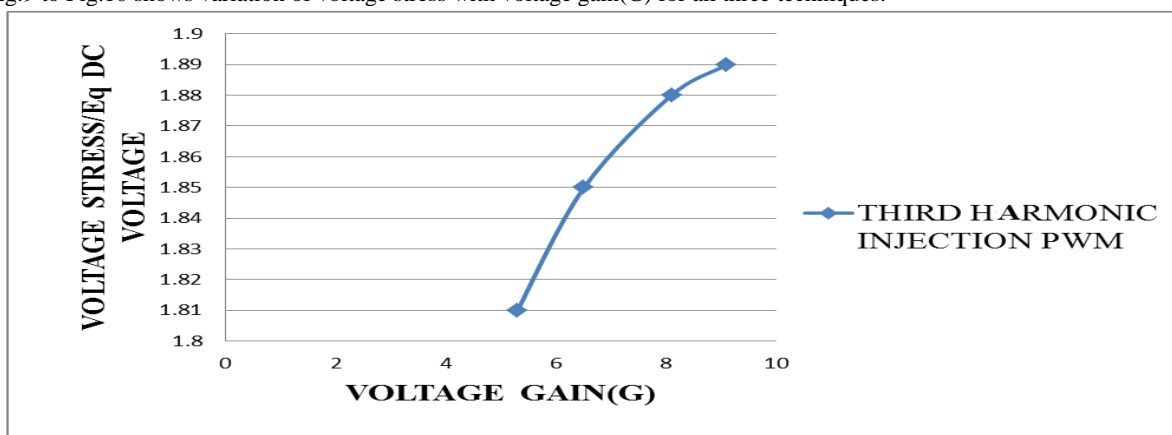


Fig 9 Effect of voltage gain on voltage stress for simple boost control method

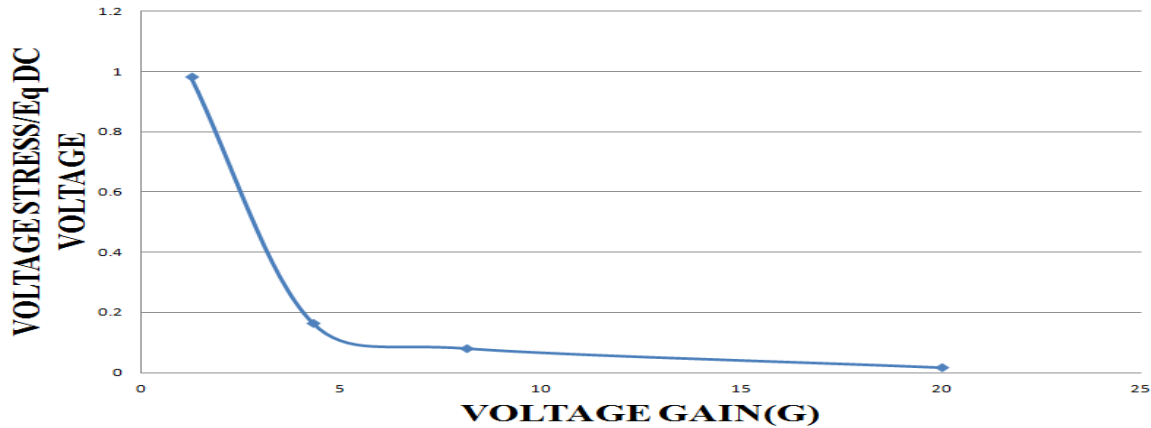


Fig 10 Effect of voltage gain on voltage stress for maximum boost control method

Table -III COMPARISON TABLE FOR THE CONTROL METHODS

S. N O	PARAMETERS	SIMPLE BOOST CONTROL METHOD	MAXIMUM BOOST CONTROL METHOD
1	THD <sub>v</sub>	6.78	5.58
2	THD <sub>i</sub>	6.62	5.16
3	Ripple in capacitor voltage	0.0414	0.1138
4	Ripple in inductor current	0.5	0.0598
5	Voltage gain(G)	9.107	20
6	Voltage stress	1.89	2.03
7	Boost factor(B)	1.25	3.09

From the Table III, it is observed that the maximum boost control method has less Capacitor voltage ripple which reduces the cost of the capacitor used and gives high voltage gain (G) and reduced voltage stress ( $V_s$ ) compared to simple boost control. Inductor rating of maximum boost control method is reduced with third harmonic injection PWM technique and also ripple in the output current reduces thus reducing the cost of the filter. With this maximum boost control method, THD of the output voltage waveform has been reduced. Therefore maximum boost control method is preferred for the proposed topology.

## V. CONCLUSION

This paper provides a clear overview on control techniques used in z-source multilevel inverters. It has been found that the maximum boost control method yields better results when compared to maximum boost control method. By employing the maximum boost control technique THD of the output voltage is reduced, inductor rating is reduced with third harmonic injection PWM technique, capacitor voltage ripple is less which reduces the cost of the capacitor used, ripple in the output current reduces thus reducing the cost of the filter, high voltage gain (G) and reduced voltage stress  $V_s$ . The impact of third harmonic injection has eliminated 3<sup>rd</sup> order harmonic and multiples of 3<sup>rd</sup> order harmonics there by reducing the output voltage THD (THD<sub>v</sub>) and output current THD (THD<sub>i</sub>).

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### Biography



**Dr. R. Seyezhai** obtained her B.E. (Electronics & Communication Engineering) from Noorul Islam College of Engineering, Nagercoil in 1996 and her M.E in Power Electronics & Drives from Shanmugha College of Engineering, Thanjavur in 1998 and Ph.D from Anna University, Chennai, in 2010. She has been working in the teaching field for about 14 Years. She has published 100 papers in the area of Power Electronics & Drives. Her areas of interest include SiC Power Devices & Multilevel Inverters.



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