Fractal Image Compression of Satellite Imageries using range and domain technique

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Abstract—Fractal coding is a novel method to compress images, which was proposed by Barnsley, and implemented by Jacquin. It offers many advantages. Fractal image coding has the advantage of higher compression ratio, but is a lossy compression scheme. The encoding procedure consists of dividing the image into range blocks and domain blocks and then it takes a range block and matches it with the domain block. The image is encoded by partitioning the domain block and using affine transformation to achieve fractal compression. The image is reconstructed using iterative functions and inverse transforms. In the present work the fractal coding techniques are applied for the compression of satellite imageries. The Peak Signal to Noise Ratio (PSNR) values are determined for images namely Satellite Rural image and Satellite Urban image. The Matlab simulation results for the reconstructed image for 4 iterations show that PSNR values achievable for Satellite Rural image ~17.0 and for Satellite urban image ~22.

Keywords—Fractal; quad-tree; iterated function system (IFS); image compression

I. INTRODUCTION

Fractal image compression is a new method to compress images. Unlike conventional method its purpose is to reduce redundancy between blocks. It was proposed by Barnsley in 1988 [1], and implemented by Jacquin [6, 7]. It is based on the theory of iterated function systems (IFS) theory developed by Hutchinson [4] and Barnsley [2]. By far there are lots of published work, such as [5, 8, 9], and the book [3]. The basic idea of the method is as follows. At first, an image is partitioned into non-overlapping blocks, which are called range blocks. Then for each range block a contractive affine transformation and a domain block are determined so that the result block generated by applying the affine transformation to the domain block is similar enough to the range block. The domain block of a transformation should be larger in area than its corresponding range block in order for the transformation to be contractive. At last, all the contractive affine transformations, which just compose contractive IFS, consist of a code of the image. When decoding, the code is iterated repeatedly on any starting image, and the result image is just the decoded image. In general the number of iterates is 6 to 8. Simulation results show that the runtime of the proposed algorithm is reduced greatly compared to the existing methods. At the same time, the new algorithm also achieved high PSNR values. Fractal coding is a novel method to compress images. It offers many advantages. In [10] proposes a new method using best polynomial approximation to decide whether a domain block is similar enough to a given range block. Also gives a kind of domain pool. It is found that the probability distribution of 8 isometrics in the fractal code is not average. And consequently it is proposed to use only 2 or 4 isometries to speed up compression.

The paper is organized as follows. Section 2 describes the Fractal compression technique. After this, section 3 presents the affine transform. Then section 4 gives mathematical foundation of IFS in [2].

Section 5 describes the proposed algorithm used in this paper.

II. FRACTAL COMPRESSION

There are several different ways to approach the fractal compression. One way is to use the fixed point transformation. A function f(.) is said to have a fixed point x₀ if f(x₀) = x₀. Suppose the function f(.) to be of the form ax + b. Then, except for when a = 1, this equation always has a fixed point.

\[ ax_0 + b = x_0 \] 
\[ x_0 = (1-a) \cdot b \]  
(1)

This means that to transmit the value of x₀, using the values of ‘a’ and ‘b’ and obtain x₀ at the receiver using (1). Instead of solve this equation to obtain x₀, we could take a guess at what x₀ using recursion

\[ x_0(n+1) = a \cdot x_0(n) + b \]  
(2)

Thus, the value of x₀ is accurately specified by fixed point equation. The receiver can retrieve the value either b the solution of (1) or via the recursion (2). In this paper we partition the image into blocks Rk, called range blocks, and obtain a transformation fₖ for each block. The transformations fₖ are not fixed point transformations since they do not satisfy the equation \( f_k(R_k) = R_k \). Instead, they are a mapping from a block of pixels Dₖ from some other part of the image. While each individual mapping fₖ is not a fixed point mapping, that can combine all these mappings to generate a fixed point mapping. The image blocks Dₖ are called domain blocks, and they are chosen to be larger than the range.
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blocks. The domain blocks are obtained by sliding a K X K window over the image in steps of K/2 or K/4 pixels. The transformations fk are composed of a geometric transformation gk and a massif transformation mk. The geometric transformation consists of moving the domain block to the location of the range block and adjusting the size of the domain block to match the size of the range block.

\[ \hat{R}_k = f_k(D_k) = m_k(g_k(D_k)) \quad \ldots \quad (3) \]

\( \hat{R}_k \) instead of \( R_k \) in (3) because it is not possible to find an exact functional between domain and range blocks, since some loss of information. This loss is measured in terms of mean squared error. In order to reduce the computations, restrict the number of domain blocks to search. However, in order to get the best possible approximation, the pool of domain blocks to be as large as possible. The elements of the domain pool are then divided in to shade blocks, edge blocks, and midrange blocks. The shade blocks are those in which the variance of pixel values within the block is small. The edge block, contains those blocks that have a sharp change of intensity values. The midrange blocks are those that fit into not too smooth but with no well defined edges. The encoding procedure proceeds as a range block is classified into one of the three categories described above. If it is a shade block, send the average value of the block. If it is a midrange block, the massic transformation is of the form ( \( ok \ tij + \Delta k \) )

where \( Tk = g_k(D_k) \), and \( tij \) as the \( ij \)th pixel in \( Tk \). \( i = 0, 1, \ldots, M-1 \), \( ok \) is selected from a small set of values. Thus the possible values of \( a \) and the midrange domain blocks in the domain pool order to find the \( (ok \ Dk) \) pair that will minimize \( d(R_k, ok \ Tk) \). The value of \( \Delta k \) is then selected as the difference of the average values of \( R_k \) and \( ok \ Tk \). If the range block \( R_k \) is classified as an edge block. The block is first divided into a bright and a dark region. The dynamic range of the block \( rd(R_k) \) is the computed as the difference of the average values of the light and dark regions. For a given domain block, then used to compute the value of \( ok \) by

\[ ok = \min\{(rd(R_k))/\epsilon, \alpha_{\max}\} \quad \ldots \quad (4) \]

In (4) \( \epsilon \) is an upper bound on the scaling factor.

The work carried out in the paper is based on range and domain technique. Taking different images such as satellite Rural and satellite urban images of size 128 X 128 pixels for fractal compression. The PSNR is calculated for the reconstructed image for the various Range block.

III. AFFINE TRANSFORMATION

An affine transformation \( w: \mathbb{R}^n \rightarrow \mathbb{R}^n \) can always be written as \( w = Ax + b \), where \( A \in \mathbb{R}^{n \times n} \) matrix and \( b \in \mathbb{R}^n \) is an offset vector. Such transformation will be contractive exactly when its linear part is contractive, and this depends on the metric used to measure distances. A linear transformation can scale with \( A_s \), stretch with \( A_t \), skew with \( A_u \), and rotate with \( A_\theta \).

IV. MATHEMATICAL FOUNDATION OF IFS

Let \( (M, d) \) is a complete metric space. A transformation \( \omega: \mathbb{R}^n \rightarrow \mathbb{R}^n \) is contractive if there exists a constant \( 0 < \epsilon < 1 \) such that

\[ d(\omega(u), \omega(v)) \leq \epsilon d(u, v), \quad \forall u, v \in \mathbb{R}^n, s \text{ is called contractility factor. An iterated function system (IFS) consists of a complete metric space} (M, d) \text{ and a set of contractive transformations } T_i, i = 1, 2, \ldots, N, \text{ where contractility factor of } T_i \text{ is } s_i. \text{ We define } \mathcal{I} \text{ as } \mathcal{I}(\nu) = \nu(i=1\rightarrow N) T_i(\nu), \quad \forall \nu \in \mathbb{R}^n \]

It can be proved that \( \mathcal{I} \) is a contractive transformation, and its contractility factor is \( s = \max \{s_i\} \). According Banach’s fixed point theorem, \( \mathcal{I} \) has a unique fixed point \( \mu \in \mathbb{R}^n \), such that \( \mathcal{I}(\mu) = \mu \).

The IFS model generates a geometrical shape with an iterative process. An IFS based modelling system is defined by a finite set of \( \mathcal{I} \) with operators \( T_i \in s \). The algorithm steps are as follows.

V. THE PROPOSED ALGORITHM

1. Divide the original image into Range block size, do not overlap. Taking of fixed dimension of Range block as 16x16, 8x8, 4 X 4.
2. Take Domain block Di twice the size of the Range block Ri in the original image.
3. Partitioning the Domain blocks doing scaling, averaging, rotation and calculating contrast that is affine transformations Di1 to Domain block Di.
4. Calculate the root of mean square of Range block Ri and each corresponding transformed Domain block Di1, as the matching error \( d \) between the two blocks. If the matching error to satisfy \( d < \epsilon \), \( \epsilon \) is a present tolerable error, skip to step6.
5. If a full search completed, and did not meet the conditions \( d < \epsilon \), segment the original block Ri into four equal, repeat (2) to (6) operations.
6. Record the fractal coding information to complete a fractal encoding.
For the encoding image applying iterations and inverse transform to reconstruct the image and calculating PSNR.

VI. RESULTS AND DISCUSSIONS

The algorithm realized in Matlab to code and to decode the satellite image of Urban of size 1377 X 955, rural image of size 995 X 57. But all these images are resized to 128 X 128. Experimental parameters are listed as Range block of size is 4, 8, 16 and number of iterations. The compression ratios and the PSNR values obtained for the reconstructed Satellite Rural Image and Satellite Urban Image is listed in Table 1. The original image and the reconstructed image after fractal encoding- decoding is shown in Figure 1 and 2.

Table 1: RESULT FOR URBAN IMAGE

<table>
<thead>
<tr>
<th>RANGE SIZE</th>
<th>ITERATION</th>
<th>PSNR(db)</th>
<th>COMPRESSION RATIO</th>
</tr>
</thead>
<tbody>
<tr>
<td>16</td>
<td>8</td>
<td>17.01</td>
<td>11.0</td>
</tr>
<tr>
<td>8</td>
<td>8</td>
<td>17.86</td>
<td>10.5</td>
</tr>
<tr>
<td>4</td>
<td>8</td>
<td>21.93</td>
<td>3.2</td>
</tr>
</tbody>
</table>

Table 2: RESULT FOR RURAL IMAGE

<table>
<thead>
<tr>
<th>RANGE SIZE</th>
<th>ITERATION</th>
<th>PSNR(db)</th>
<th>COMPRESSION RATIO</th>
</tr>
</thead>
<tbody>
<tr>
<td>16</td>
<td>8</td>
<td>13.53</td>
<td>15.01</td>
</tr>
<tr>
<td>8</td>
<td>8</td>
<td>15.89</td>
<td>12.8</td>
</tr>
<tr>
<td>4</td>
<td>8</td>
<td>18.01</td>
<td>3.2</td>
</tr>
</tbody>
</table>

It is clearly seen from the Table 1 and Table 2 that for a compression ratio ~3.2 the PSNR values achievable for Satellite Rural Image and Satellite Urban image are different. The Rural image ~18.01 and the Urban image ~21.93. The Urban image shows the highest PSNR values compared to rural image. Further it can be seen from the Figures that the reconstructed urban image has a better quality of the reconstructed image compared to that of rural image. These results suggest that the urban images contain more fractal information compared to that of rural image. The fractal coding techniques are better suited for the compression of satellite urban images.
VII. ACKNOWLEDGEMENTS

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